

Section 1: Algebra

- 1.1 a.
- 1.2 all.
- 1.3 $\pm 1, \pm i$.
- 1.4 1, 2.
- 1.5 e.g. $x^3 + 2x + 1$.
(any polynomial of degree 3, for which 0, 1 and 2 are not roots (mod 3)).
- 1.6 (a) n ; (b) 0.
- 1.7 a, c.
- 1.8 b, c.
- 1.9 a, c.
- 1.10 a, c.

Section 2: Analysis

- 2.1 (a) conditionally convergent; (b) divergent; (c) absolutely convergent.
- 2.2 $]0, 2]$.
- 2.3 1.
- 2.4 $1/\pi$.
- 2.5 a, c.
- 2.6 a.
- 2.7 all.
- 2.8 $8\pi i$.
- 2.9 a, b.
- 2.10 none.

Section 3: Topology

- 3.1 a, b.
- 3.2 b, c.
- 3.3 c.
- 3.4 c.
- 3.5 b.
- 3.6 a, c.
- 3.7 c.
- 3.8 Yes; uncountable.
- 3.9 Yes.
- 3.10 Yes; 1.

Section 4: Applied Mathematics

4.1 $\frac{4}{3}\pi a^3$.

4.2 $\operatorname{div} u = 0$.

4.3 0.

4.4 π^2 .

4.5

$$\frac{1}{2}\ell^2 \left(\frac{d\theta}{dt} \right)^2 = g\ell(\cos \theta - \cos \alpha)$$

4.6 $u(x, t) = x^2 + t^2$.

4.7 $\min z = 4$ at the point $(8/7, 4/7)$. (Either data can be accepted as full answer).

4.8 a, b.

4.9 $L[f](p) = a/(a^2 + p^2)$.

4.10

$$\int_{\Omega} f \, dx + \int_{\partial\Omega} g \, dS = 0.$$

Section 5: Miscellaneous

5.1 $\frac{n}{2} \sin \frac{2\pi}{n}$.

5.2 $8t^4 - 8t^2 + 1$.

5.3 $2/3$.

5.4 $4/9$.

5.5 all.

5.6 01.

5.7 960.

5.8 Example: $(n + 1)! + 2, \dots, (n + 1)! + (n + 1)$.

5.9 5.

5.10 40.